

OBSERVE: Occupancy-Based System for Efficient Reduction of HVAC Energy

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ABSTRACT

Heating, cooling and ventilation accounts for 35% energy usage in the United States. Currently, most modern buildings still condition rooms assuming maximum occupancy rather than actual usage. As a result, rooms are often over-conditioned needlessly. Thus, in order to achieve efficient conditioning, we require knowledge of occupancy. This paper shows how real time occupancy data from a wireless sensor network can be used to create occupancy models which in turn can be integrated into building conditioning system for usage based demand control conditioning strategies. Using strategies based on sensor network occupancy model predictions, we show that it is possible to achieve 42% annual energy savings while still maintaining American Society of Heating, Refrigerating and Air-Conditioning (ASHRAE) comfort standards.

Categories and Subject Descriptors

I.6.5 [Simulation and Modeling]: Model Development;
J.7 [Computers In Other Systems]: Command & control

General Terms

Algorithms, Machine Learning, Measurement

Keywords

Occupancy, HVAC, Ventilation, Energy savings

1. INTRODUCTION

In 2006, approximately 35% of the energy in the United States was used for heating, ventilation, and air-conditioning (HVAC) systems[2]. Studies suggest that 15% to 25% of HVAC energy can be saved by setting ventilation rates based on maximum occupancy [8]. Currently, the majority of HVAC systems condition rooms assuming maximum occupancy during normal working hours and are turned off at night. This leads to inefficiency as rooms are often conditioned to levels that are not appropriate for the number of

occupants actually occupying the areas. An HVAC could waste energy supplying ventilation enough for 30 people when only 10 actually occupy a room.

To increase the efficiency of HVAC systems, a system for detecting occupancy is needed to condition rooms appropriate to usage. Though there are several methods that are commonly used for detecting occupancy within modern buildings, these methods present limitations. Passive infrared (PIR) sensors, commonly used for controlling lighting, are a simple way of detecting if a room is occupied or not, but do not give information regarding how many people occupy the room. This information is necessary for CO₂ ventilation. Using CO₂ sensors directly for regulating CO₂ is also unsuitable for conditioning strategies. CO₂ buildup is slow, and by the time sensors detect high levels of CO₂ that trigger ventilation, occupants of the room are likely to already feel uncomfortable [13]. If not properly calibrated, these sensors can also be inaccurate [13]. Electrical loads have also been used for occupancy estimation [6]. However, this method assumes each occupant contributes to the load and requires accurate occupancy data for calibration.

For demand response HVAC control, occupancy detection needs to be accurate, reliable, and able to capture occupancy changes in real time. The Smart Camera Occupancy Position Estimation System (SCOPEs) [15] is a 16 node sensor network of cameras that captures occupancy changes among areas with approximately 80% accuracy in near real time. With newer more powerful hardware it is likely the accuracy will be even greater.

Though the ability to adjust an HVAC system based on real time occupancy is an important step toward greater efficiency, perhaps just as important is the ability to anticipate room usage based on current room usage. This needs to be addressed since conditioning a room is not instantaneous and requires time for adjustments. For example, if it is known that a large number of people are in a lobby area, we want the HVAC system to know an adjacent conference room will be used with high probability and begin conditioning the room beforehand.

The following are the key contributions of our work:

1. Our work on occupancy modeling uses inter-room relationships over time to model occupancy. In addition, our models are developed using accurate real world data rather than occupancy walk-through surveys or other similar estimates of occupancy.
2. We demonstrate how models developed from sensor network data can be integrated with an HVAC control strategy to achieve significant energy savings.

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3. We show that we can still satisfy ASHRAE conditioning standards while saving significant energy. In certain cases, we show that our predictive strategies meet user demand better than typical baseline strategies.
4. We examine a PIR based WSN solution and show that binary measurement of occupancy is not always sufficient for HVAC control. Under some circumstances, PIR based HVAC control performs worse than current strategies; in order to achieve maximum energy savings within a building, *accurate real time levels of occupancy must be incorporated into HVAC strategies.*

2. RELATED WORK

Few works on occupancy modeling have been published that are relevant to demand control systems. Most acknowledge that a major obstacle for developing occupancy prediction models is lack of data. It is time consuming to gather ground truth occupancy data even for a small set of rooms.

The simplest and most commonly used occupancy models are sets of predefined static coefficients that are multiplied with a maximum room occupancy. To estimate the occupancy of a room at 8am given that the room has a maximum occupancy of 30, the coefficient for 8am is simply multiplied with 30. Different sets of coefficients are used depending if it is a weekday, weekend, or holiday and the purpose of the building. ASHRAE Standard 90.1 [5], BLAST [14], and DOE-2 [1] define several occupancy profiles for office buildings daytypes. These models are commonly used for energy simulation tools such as eQuest [11] or EnergyPlus during the design phase of buildings and are also used to determine static conditioning strategies for buildings.

Several methods of modeling occupancy do so using multiple sources of sensory input. In [6], the authors shows how occupancy can be modeled using linear regression models. Data was collected for lighting and equipment loads and occupancy is estimated using a walkthrough survey of the building. Using the electrical loads as the indicator variables and occupancy estimations as the response variable, linear regression models for weekdays, weekends, and holidays were created. The main limitation of this model is the reliance on energy usage to determine if someone is present. In general, it will tend to underestimate occupancy levels. For example, occupants attending a large group meeting in a conference room may not be adding any additional loads causing the model to report the room empty. Occupancy prediction for conditioning is also difficult as it would first require the ability to predict electrical loads.

The authors of [7], utilize a deployment of PIR and door sensors to obtain a binary indication of occupancy. They use a reactive strategy that adjusts the temperature based on current occupancy and estimate potential savings using EnergyPlus. This ignores the ramp up time required for a room to be brought to temperature. The paper also does not account for the impact of ventilation on energy savings.

In [17], the authors also utilize door and PIR sensors for binary detection of occupancy for residential buildings and examine reactive and predictive controls strategies. The predictive strategy is achieved using a Hidden Markov Model. The model estimates the probability of home being in one of three states: unoccupied, occupied with an occupant awake, and occupied with all occupants asleep. The authors provide results for real world deployment and EnergyPlus sim-

ulations. However, the results do not take into account ventilation, which can have a significant impact on energy efficiency. Also, the modeling approach does not account for different daily schedules. If a person stays out late on Friday on a semi-regular basis, the model would not be able to predictively condition for this scenario.

In [10], the authors propose using a belief network for occupancy detection within buildings. The authors use multiple sensory input to probabilistically infer occupancy. By evaluating multiple sensory inputs, they determine the probability that a particular area is occupied. In each office PIR and telephone on/off hook sensors were used to determine if rooms are in occupied states. The authors model the occupied state of individual rooms with a Markov Chain, where the transition matrix probabilities are calculated by examining the exponential distribution of the sojourn times of the observed states. While these strategies are more suitable for predictive demand control strategies, there are limitations that diminish their usefulness. The strategies are aimed for modeling occupancy for individual offices and cannot be applied to spaces with larger occupancies. Though the multiple telephone sensors could potentially be used to help determine a lower bound of occupancy, it is difficult to determine when someone leaves since the presence of multiple people essentially nullifies the usefulness of the PIR sensor. The approach does not consider room interdependencies and only focuses on occupancy detection.

In [12], an agent based model (ABM) and a multivariate Gaussian model (MVGGM) are examined. We will discuss these models in Section 4.

3. SENSING AND DATA COLLECTION

In our work, we use the SCOPES system developed by Kamthe et al. [15]. SCOPES is a system comprising 16 sensor nodes on the ceiling of the corridors a University building. Nodes were deployed at transition boundaries within the hallways of the building. Each transition boundary is comprised of a group of three nodes. Each node is a Cyclops camera interfaced with a Moteiv Tmote Sky module via an intermediate adapter board. Both pieces of hardware run TinyOs as the operating system. The Cyclops is a low power camera with an on-board 4MHz ATmega128L micro-controller (MCU) and 512KB of external SRAM. The external SRAM is divided into eight, 64KB memory banks to overcome the limitations of the addressable memory. Each bank is capable of storing 80 64x64 pixel grayscale images. At every transition boundary location, three nodes sense the same area where the nodes take turns capturing the sensed area. Whenever a person crosses any one of these transition points, the cameras capture and process the image data and determine the if a transition occurred and the direction.

Since the computational resources of the nodes are limited, only lightweight image processing algorithms are used. Object detection is achieved by background subtraction, and the background is updated continuously. When an object is detected, the pixels of the image are classified as an object, shadow, or background depending on a pre-determined threshold. All pixels classified as objects are grouped using a connected component algorithm creating a blob. The centroid and pixel count of the blob is determined and the direction is inferred by consecutive images. Once a mote has processed all images in its bank, object information is transferred to a base station using multi-hop communication.

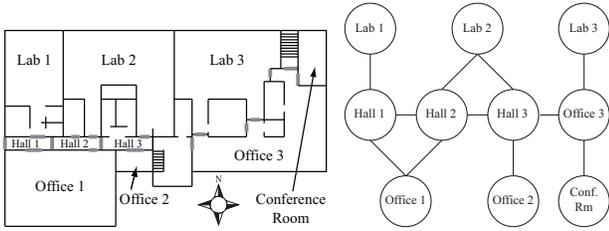


Figure 1: The left shows the ten areas data was collected for and the 18 boundaries (gray lines) defining the areas. The right shows a graph representation.

We found SCOPES was able to detect 80% of all recorded transitions within a 24 hour period of time.

3.1 Data Collection

Five days (Mon-Fri) of ground truth occupancy data were gathered for ten areas using seven cameras covering 18 transition boundaries. Figure 1 shows the building areas used for data collection. The cameras recorded images at 1.5 fps. Simple background subtraction methods were used to first help identify images containing people and then processed by hand to verify direction and the boundaries being crossed.

The hall occupancies are generally 0. When the hallway is occupied, the occupancy is usually low and the occupants typically exit within 4 to 8 seconds. There are a few instances that the hall occupancy deviate from this typical pattern. When the data was collected, there was construction work being done near Lab 1. On Monday and Thursday, about 7 people conducted building inspections in the hallway. There are also some instances where people held lengthy conversations in the hallway sections.

Figure 2 shows the occupancy data for ten areas. The Office 1, Office 3, Lab 1, and Lab 3 show occupancy patterns more typical of work routines though with some slight variations. Office 1 is used by school administration. Workers come in consistently at 8am, leave for lunch, come back from lunch, and then leave at 5pm. Office 3, Lab 1, and Lab 3 are used by professors and graduate students. Though the same general daily pattern can be seen, we can also see some occupants stay later (all night in some cases) and arrive and leave at odd hours. Office 2 and the Conference Room are similar since they both are mainly used for meetings. Office 2 is a small office that is used for student counseling meetings and certain administrative work. Lab 2 is currently not being used by any department and serves as storage space.

4. PREVIOUS MODELS

In our previous work [12], we developed an agent based model (ABM) and a multivariate Gaussian model (MVGm). The ABM simulates occupancy by modeling the behavior of the individual. Agents are given paths, walking speed, and itineraries based on the occupancy changes seen in the training data. Occupancy is simulated by creating multiple agents that follow probabilistically generated instructions. Based on their simulated movement, room occupancies over the course of the day can be estimated. While this is useful for estimating daily occupancy changes that are possible, it is difficult to use this model to predict future room usage.

The second model evaluated is a multivariate Gaussian fit of room occupancies. Hourly defined pdfs allow the calculation of the probability for a particular occupancy state occurring within a given hour. Let $O_h = (r_1 \dots r_m)$ denote

all occupancies that occur per second during hour h where $1 \leq h \leq 24$ and r_i is a vector of occupancies for room i where $i = 1 \dots m$. Let μ_i denote the average occupancy for room r_i . The means will change based on h .

We calculate a vector of means $\mu_h = (\mu_1, \dots, \mu_m)$ and covariance matrix Σ_h from O_h . Using μ_h and Σ_h , we define a probability density function (PDF) f :

$$f(O_h; \mu_h, \Sigma_h) = \frac{1}{(2\pi)^{\frac{n}{2}} |\Sigma_h|^{\frac{1}{2}}} \exp \left\{ -\frac{1}{2} (O_h - \mu_h)' \Sigma_h^{-1} (O_h - \mu_h) \right\}$$

The PDF f can give a probability of an occupancy occurring for a specific hour dataset O_h . Using this function, we can randomly draw occupancy vectors from the distribution. Given a starting occupancy, all the possible occupancies that can occur in the next timestep are examined. For each possible occupancy the probability of the occupancy occurring using the current PDF is calculated. Using these probabilities, the occupancy for the next timestep is chosen. The drawback of this method is that it causes a great deal of pacing behavior. For example, if a person leaves the office to enter a hallway at one timestep, there is a high probability that the person will re-enter the office in the next timestep. This occurs since the distribution does not take into account the behavior observed in the previous timestep. This can cause predictions to favor parts of the distribution that have high probabilities. This is particularly pronounced for rooms rarely occupied. In these cases the model rarely allows room entry and vacates the room too quickly.

In order to create a prediction model suitable for HVAC control, we need a model that captures the temporal nature of the occupancy changes along with the inter-room correlations and occupant usage of the areas. The ABM does not take into account inter-room correlations and would require an additional modeling framework to be used for predictions based on time. The MVGM considers both the temporal and inter-room correlations. However, the distributions do not take into account previous behavior and do not accurately capture the usage of seldom used rooms.

5. MARKOV CHAIN MODEL

We model the temporal dynamics of the occupancy in a building with a Markov Chain (MC). The state of the chain consists of the occupancy at each room and transitions to a new state occurs with a probability that depends only on the current state and the time. This allows us to predict the occupancy distribution at $t + \Delta t$ given the occupancy distribution at time t by multiplying the Δt times of the transition matrix. This allows us to predict when rooms will be likely occupied and begin conditioning beforehand.

The MC state at each time is represented by a vector where each component represents occupancy in a specific

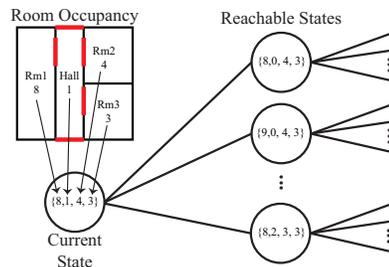


Figure 3: The occupancy state representation.

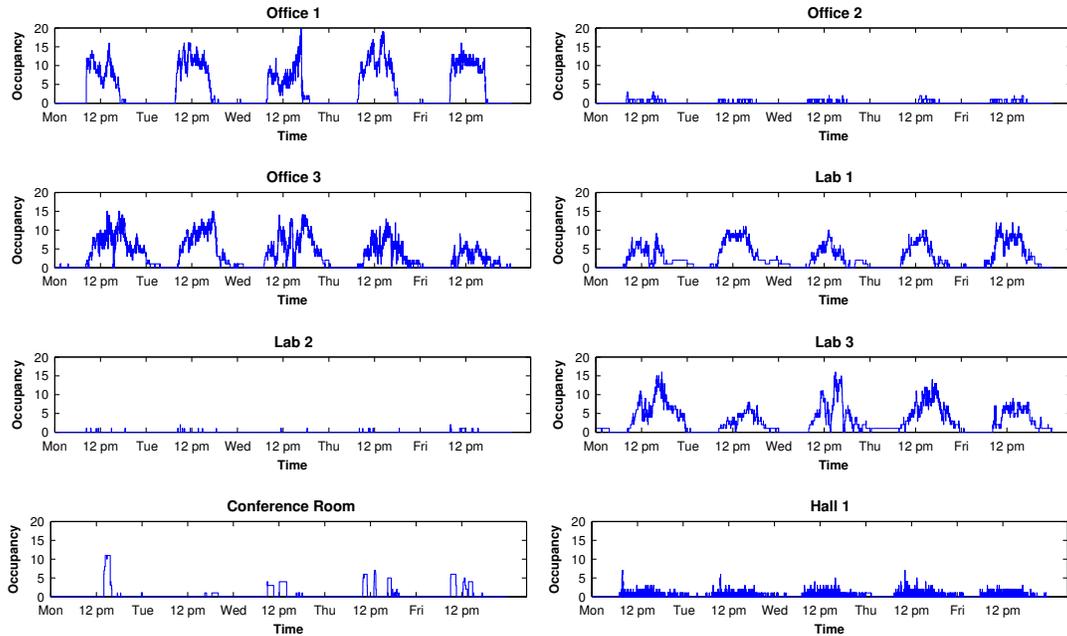


Figure 2: 5 days of ground truth occupancy data for eight areas.

room (Figure 3). Let R represent the set of n rooms to be modeled. For each room in R , there is a maximum occupancy. We define $S = \{s_0, \dots, s_m\}$ to be the set of all room occupancy combinations that are possible given the maximum room occupancies of R where m is the total number of states. Thus, S represents all observable occupancy states that can be represented by a given set of rooms R .

One issue that needs to be addressed is the potentially large state space. Assume we have $n = 4$ rooms, each with a maximum occupancy of 20 people. In this case, the MC will contain $m = 20^4 = 160,000$ states. As the number of states increases, more data is required to calculate the probabilities of the observable states. The transition matrix is sparse because many transitions are impossible due to physical constraints of the building. However, the fact still remains that as more rooms are added, the number of states to manage increases exponentially. To reduce the component cost, we define the MC only on the states that were actually observed during training. Although we will not be able to generate transitions to all observable states, practically our model will be realistic if using a large enough training set. As the WSN gathers data over time, more of the state space will be represented. Additional strategies of reducing the state space are addressed in Section 5.3.

With the observable states of the MC defined, we next define the transition probability matrix. Let p_{ij} represent the probability of moving from state j to i where X_t represents an occupancy state at time t . For each state in S we calculate $p_{ij} = P(X_{t+1} = i | X_t = j)$. Since the training data collected is at the resolution of seconds, each time step of the MC represents 1 second. The transition probabilities are estimated from the data normalized counts: $p_{ij} = n_{ij} / \sum_{k=1}^m n_{ik}$ where n_{ij} is the number of times a transition from state i to state j in the set, and m is the total number of states.

Since certain occupancy changes occur with greater probability depending on the time of day, the time of day must be incorporated into the model. Consider a person standing

in a hallway at 8:00 am. Since it is early in the day, it is likely that the person has arrived for work and will move into either a lab or office. However, if we consider the same scenario at 8:00 pm, it is more likely that the person will exit the hallway in order to leave the building. To incorporate time into the model, we define multiple transition matrices that govern the state changes within different slots of time, thus defining an inhomogeneous MC.

While considering only observed (as opposed to observable) states and multiple transition matrices does allow us to model occupancy dynamics efficiently, a problem arises. Since we only consider states observed in the training data, partitioning the data in temporal sets will create discontinuities at the slot boundaries. Suppose we partition the data to create hourly transition matrices and are predicting occupancy for hours h and $h + 1$. After 3600 steps (one hour), we are in some state X , the hour changes from h to $h + 1$, and the model switches to the hourly transition matrix for $h + 1$. It is possible the transition matrix for hour $h + 1$ has no probability for occupancy state X . This occurs if state X never occurs in the training data for hour $h + 1$. Even though in reality the state X can occur in hour $h + 1$, if X does not occur in hour $h + 1$ of the training data, then we cannot calculate the transition probabilities for X . This cannot be solved by introducing a small epsilon probability value of transitioning into another state because the next state chosen may also not be represented in the transition matrix. The MC becomes a random walk until it enters a state that was captured by the training data.

Similarly sink states can also occur if an occupancy state only occurs once in the training set. Suppose we have a set of occupancy states O that we use to train a transition matrix. Let X be the last occupancy state of the training set of O . If X is a unique state in O , then X never transitions to any other state. If the occupancy state transitions to X , it will remain in that state until the model changes to a transition matrix that does contain a transition probability. We propose two different methods of solving the boundary

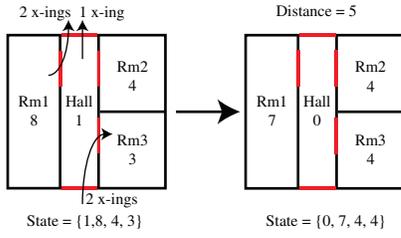


Figure 4: Example of the closest distance metric with state (Hall, Rm1, Rm2, Rm3) and distance 5.

discontinuities and avoiding sink states.

5.1 Closest Distance Markov Chain

The closest distance Markov Chain (CDMC) attempts to solve the discontinuities the time slot boundaries. Suppose we finish simulating hour h and are currently in state X . Before switching to the transition matrix for $h + 1$, we first check to see if it contains a probability for X . If the probability does not exist, then we examine all the states of transition matrix $h + 1$ that does have a probability and choose the state closest to X .

We define the distance between two states to be the number of transition to or from the outside world in order to account for the difference between the states. Let M_i represent the minimum number of area transitions that is needed for a single person to enter or exit out of a building from room i . Let $X = (x_0, \dots, x_n)$ and $Y = (y_0, \dots, y_n)$ represent two occupancy states where x_i and y_i are the occupancies of room i . We define distance $d_{X,Y}$ between X and Y to be $d_{X,Y} = \sum_{i=0}^n M_i |x_i - y_i|$. Figure 4 shows an example of this distance metric. For this four room example, the distance between the states is 5. One transition boundary is crossed to leave Hall. Two transitions crossings are needed for the person to leave Rm1. Two transition crossings are needed for the person to enter Rm3. Rm1 and Rm2 require two transitions each since a person must first enter the hallway and then from the hallway exit to the outside world.

Although this method eliminates sink states at the hourly breaks, it does not guarantee that the sequence of states is valid. It is possible for people to “teleport” in or out of areas. Consider the floor plan in Figure 4. Suppose we have the state (0, 0, 0, 0) (all the rooms are empty) and the closest state is (0, 0, 2, 0) (two people are in the office). The transition from (0, 0, 0, 0) to (0, 0, 2, 0) is impossible since the two people must first pass through the hallway to enter the office. Also, it is still possible to enter sink state in the middle of a prediction. Applying the closest distance metric again does little to help since it will likely choose the previous state and then immediately re-enter the sink state.

5.2 Blended Markov Chain

Sink states only occur when the next transition matrix does not contain a probability for the current state. In order to avoid sink states, we wish to ensure that a transition probability for the current state is always available. Rather than only consider states within the hourly transition matrix, we instead blend each matrix into a single state space containing each state of each transition matrix.

If the day is partitioned in K parts, then we have K transition matrices $T_1 \dots T_K$ each with m states. We now linearly combine these K transition matrices to obtain K blended transition matrices $\bar{T}_1, \dots, \bar{T}_K$, as follows. The blended transition matrix for slot t is

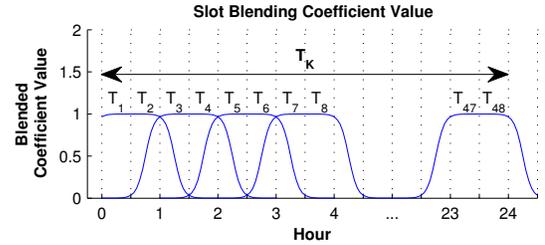


Figure 5: Relationship of blending coefficient, hourly time slot, and transition matrices.

$$\bar{T}_t = \sum_{s=1}^K \beta_{ts} T_s \quad (1)$$

where the coefficients $\beta_{t1}, \dots, \beta_{tK}$ are positive and sum to one (so that \bar{T}_t is a valid transition matrix). We want these coefficients to be approximately 1 for close slots and quickly decrease to 0 for farther slots. We can achieve this by defining the coefficients as

$$\beta_{ts} = \frac{\alpha(c_t - c_s)}{\sum_{s'=1}^K \alpha(c_t - c_{s'})} \quad (2)$$

where c_t, c_s are the centers of slots t, s , and with a “slot” function

$$\alpha(x) = \sigma\left(\frac{2a}{d}\left(x + \frac{d}{2}\right)\right) - \sigma\left(\frac{2a}{d}\left(x - \frac{d}{2}\right)\right) \quad x \in \mathbb{R} \quad (3)$$

where $\sigma(x) = 1/(1 + e^{-x})$ is the sigmoid function, $a > 0$ is the slope at the slot boundaries and $d > 0$ is the slot width. Since the sigmoid is monotonically increasing and satisfies $\sigma(-x) = 1 - \sigma(x)$, it follows that $\alpha(x)$ is positive and symmetric around its center. Figure 5 shows the slot functions for several slots. This way, each entry in the blended transition matrix \bar{T}_s incorporates information from all slots, but heavily weighting slot s .

For our model, we choose $K = 48$, partitioning the data into half hour transition matrices with slot widths of $d = 3$. We set a slope of $a = 10$ at the boundaries. We choose the c_k to be center of the current hour. Figure 5 shows the blending coefficient for these particular parameters. By defining the parameters in such a manner, we create overlapping slot boundaries. This increases the number of preferred states available to transition into, and decreases the chance of choosing states completely outside the slot boundaries. The coefficient heavily favors transitions to states within a given hour time slot and somewhat considers states in the adjacent half-hour slots. States outside this time frame are still considered, but with greatly reduced probability. These parameters were chosen through trial and error. The criteria of the parameter selection was to maximize slot size while minimizing the transitions into states completely outside the preferred slot boundaries. While larger values of K could be used, smaller values of K are preferred since a large K reduces the slot size and the number of observed states for each transition matrix. We also prefer to only draw from states that are close with respect to time.

5.3 Large Building Scalability

The number of observable states increases exponentially with the number of rooms, but as described earlier we limit the complexity of our model by using only states observed in the data sample. If this has length s over a given time period, then the number of observed states N satisfies $N \leq s$,

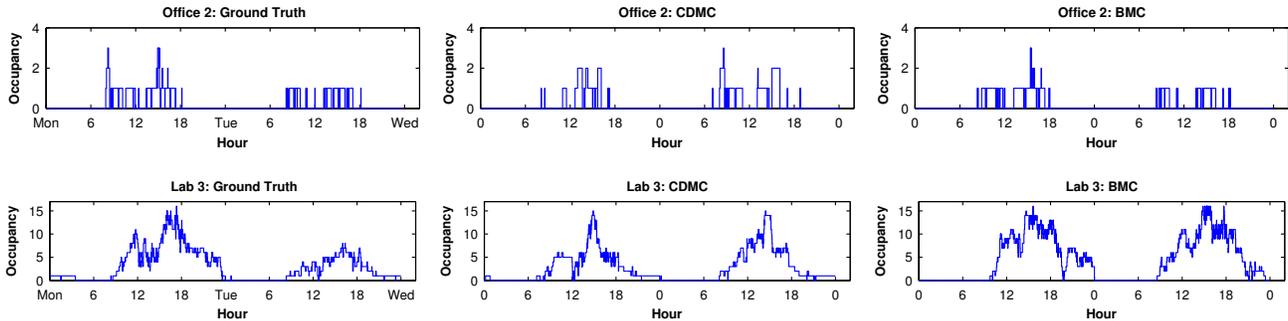


Figure 6: Comparison of training data with the models for several areas.

and practically $N \ll s$ because of repeated states. Besides, the $N \times N$ transition matrix T is typically sparse, because physical constraints make many transitions impossible and because not every possible transition is observed in the sample anyway. Indeed, the number of nonzeros in T must be smaller than s , and again is practically much smaller than s because of repeated transitions. For our 5-day training set, we observed $s = 432K$ samples resulting in $N = 3809$ and 19578 nonzero transitions ($= 0.14\%$ of all N^2 transitions).

It is conceivable that, with a very large number of rooms and a very long sample, N or the number of nonzeros of T are prohibitively large. Several simple strategies can be used to achieve a manageable model. Firstly, s should not be larger than necessary to achieve a sufficiently accurate model. Another strategy for managing the number of states is to utilize multiple MC models. Suppose we have a building with 40 rooms that is divided into two wings each containing 20 rooms. Rather than have a state representation that includes all 40 rooms, we can train one MC per wing. The trade off is that more MC models would be required to describe all possible relationships of all the rooms. Lastly, it is often possible to aggregate multiple rooms together thus reducing the number of states. This is because HVAC systems typically condition groups of rooms called zones. We can aggregate room occupancies within a zone, and then create an MC model using zones rather than individual rooms.

6. MARKOV CHAIN PERFORMANCE

In this section we will examine how well BMC and CDMC capture room occupancy. For each model, 100 simulations of 24 hours were created. Five days (Mon-Fri) of ground truth occupancy data was used to train the models. An additional three days (Mon, Wed, Fri) of ground truth data is used for testing. Figure 6 shows two days of training data along with model simulated room occupancy schedules. Even without formal tests, the models seem to be capturing the dynamics of the ground truth room occupancies. As expected, the CDMC enters sink states and remains in the state until the end of the hour. Qualitatively, BMC seems to model occupancy variability better than CDMC.

6.1 Comparison Metrics

We use three metrics to evaluate the quantitative performance of the models. We first examine how long room occupancies remain static to measure occupancy variability. We expect our occupancy models to remain at the different levels of occupancy for similar durations as compared with the ground truth data. The next metric utilizes Jensen-Shannon divergence (JSD). This is a method that applies Kullback-Leibler divergence (KLD) to compare the similar-

ity of two distributions. The advantage of JSD over KLD is that JSD will always return a finite value and is symmetrical. We compare the room occupancy distributions of the models and testing data for different windows of time during the day. The last metric considered is the rate people enter and exit a room. By examining the durations between entrances and exits of a room, we can measure the flow of occupants in and out of a room. Specifically, for a window of time w , we calculate $\lambda_{in,w}$ and $\lambda_{out,w}$ for each room where the variables represent the rate of flow in and the rate of flow out of a room respectively. Time is taken into account since the rate of flow changes depending on the time of day.

6.2 Evaluation

Figure 7 compares the average static durations of the various occupancy levels with those seen in the testing set. Duration differences closer to 0 indicate a closer fit to testing data. For high traffic areas and rooms with low occupancy, BMC and CDMC show similar differences. CDMC typically shows larger differences of durations since the CDMC still tends to get stuck in states near the ends of the hourly partitions. This causes the occupancy level to remain static for periods of time longer than normal. Areas with larger occupancies are prone to containing sink states as more data is required to cover the possible state space. This can be seen in Figure 7 for Office 1 where CDMC remains at several occupancy levels for long durations. Similar results were found for the other areas with higher levels of occupancy such as Office 1, Office 3, Lab 1, and Lab 3.

We next examine the JSD for the different models. We partition the day into 2 hour slots and examine the JSD for each window of time. Examining the ground truth data in Figure 2, we can expect a fair amount of variation among different days. To establish a baseline of how much divergence is typical from day to day, we compare the occupancy distributions of each testing set day to the remaining testing set days for each window of time and establish the maximum divergence for each time slot. Rooms that are mostly empty such as Lab2 and the conference room have JSD of nearly 0 for each window of time. Figure 8 shows the JSD for the rooms that are consistently occupied. When we compare the testing set for each model, we see that the JSD for each window is consistent. We find that both models have JSD's that are below the maximum observed JSD.

Lastly we examine the flow of occupants for each room. We consider the hours 7am - 10am to be morning, 11pm - 2pm to be afternoon, and 3pm - 6pm to be evening. Based on these windows of time, we calculate the flow into and out of rooms. Figure 9 shows the flows into Hall 1 and Office 1 for the different simulations. As with JSD, we will use the

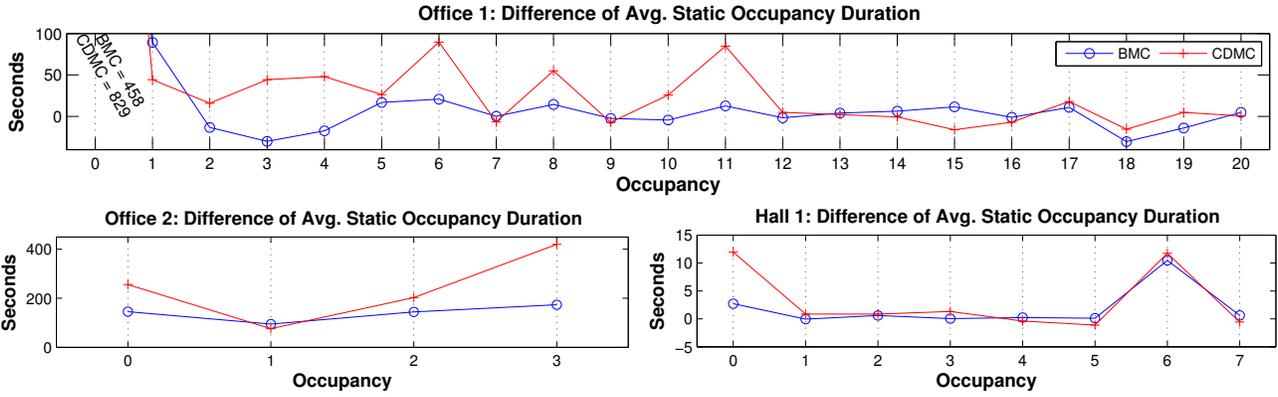


Figure 7: The difference of the average static occupancy duration from 7am - 10pm.

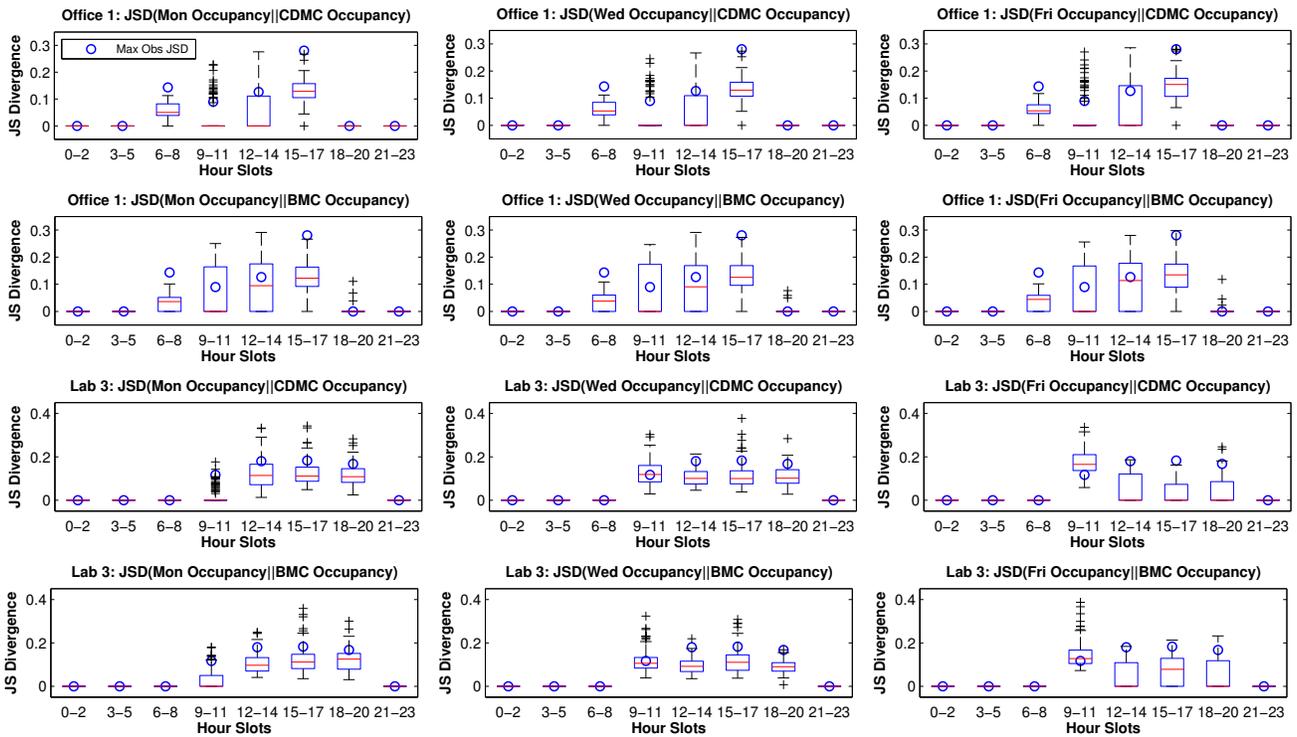


Figure 8: Each boxplot is for the JSDs observed within the time slot where the + is an outlier.

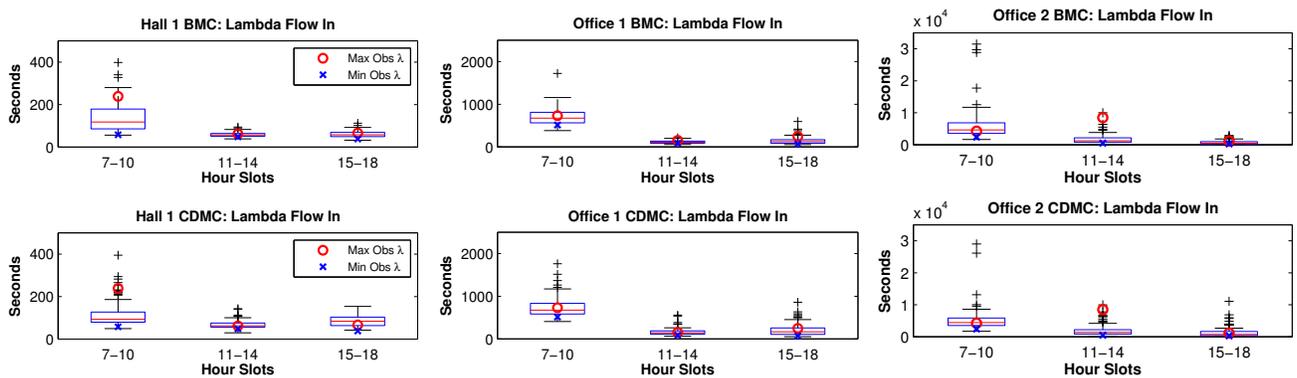


Figure 9: Flows for Hall 1, Office 1, and Office 2 and the min and max flows observed in the testing set.

ground truth test data to establish upper and lower limits for the λ values. Again, both BMC and CDMC simulations fall mostly within the limits. However, CDMC tends to have more outliers, which again is caused by sink states.

Overall, both models perform well, but in general, BMC performs better since it does not encounter discontinuities at the boundaries. The sequence predicted by BMC is also always valid, which may not be the case for the CDMC.

7. HVAC CONDITIONING STRATEGIES

Using the BMC, we define a predictive control algorithm for temperature. We start by defining the thermal and ventilation criteria that our HVAC strategies must meet to have an ASHRAE compliant building. We then define the occupancy based temperature control strategy OBSERVE.

7.1 Conditioning Criteria

7.1.1 Temperature

Thermal comfort is a complex measurement that depends on many aspects such as temperature, humidity, air velocity, occupants clothing and activity [16, 19]. The most common comfort measurement is Fanger’s Predicted Mean Vote PMV as standardized in ISO 7730 [18]. Fanger’s model is not an undisputed thermal comfort measurement [18, 19, 20], but provides good generalized results in many cases. Fanger computes the thermal comfort PMV value between -3.5 and 3.5. Rounding the PMV results in the comfort classes hot ($PMV > 2.5$), warm ($1.5 \leq PMV < 2.5$), slightly warm ($0.5 \leq PMV < 1.5$), neutral ($-0.5 \leq PMV < 0.5$), slightly cool ($-1.5 \leq PMV < -0.5$), cool ($-2.5 \leq PMV < -1.5$), and cold ($PMV < -2.5$). Fanger’s PMV depends on air temperature [18], radiant temperature, humidity, air velocity, occupants clothing and activity. The model is non-linear and based on large scale studies in climate chambers.

Measuring the PMV based on this model is very complex due to the many influences. The activity and clothing level of occupants is simplified by assuming defaults such as office work and clothing level is correlated to the outside temperature [4]. However, this still requires an air temperature, radiant temperature, humidity and air velocity sensor in each room. Air temperature and simple humidity sensors could be added to our wireless sensor node, but radiant temperature and air velocity sensors are complex and expensive, such that large scale installations are not affordable. Given these complexities, our work focuses on optimally controlling temperature rather than attempting to control PMV. From a control perspective, our goal is to meet a target temperature defined by a comfort metric, which may not necessarily be Fanger PMV. Different comfort metrics will establish different temperature set-points. It is thus more important to meet specific target temperatures than to meet a specific comfort metric. As metrics are developed and better environment sensing is available, we want our system meet the temperature goals dictated by the new comfort criteria.

7.1.2 Ventilation

ASHRAE Standard 62.1 [4] uses the following to calculate outdoor air ventilation rates:

$$V_{bz} = R_p P_z + R_a A_z \quad (4)$$

where z denotes the zone, V_{bz} is the ventilation rate, R_p is the minimum CFM/person, P_z is the number of people, R_a is the minimum CFM/ft², and A_z is the floor area. The P_z

Algorithm 1 OBSERVE temperature control algorithm.

```

CondTempi,j ← Condition temperature from time i to j
CurrHour ← Current hour
TTG ← Temperature such that PMV = 0
TASH ← Temperature such that -0.5 < PMV < 0.5
pThresh ← Probability threshold of occupancy

```

```

for Every n minutes do

```

```

  CurrOcc ← Current occupancy state
  occPred ← BMC(CurrOcc, predLen)

```

```

for Each room r and point of time t in occPred do

```

```

  occupied ← All periods occPredt→t+60 > pThresh

```

```

  if occupied > 5 minutes of next 15 minutes then

```

```

    CondTempt-60,t+15 = TTG

```

```

  else if occupied > 20 minutes of next 60 minutes then

```

```

    CondTempt-60,t+60 = TTG

```

```

  else if 5 ≤ CurrHour ≤ 24 then

```

```

    CondTempi,i = TASH

```

```

  end if

```

```

end for

```

```

end for

```

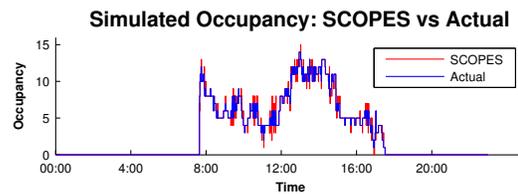


Figure 10: Simulated SCOPEs data.

by determining A_z . The other constants are determined by ASHRAE Standard 62.1.

7.2 OBSERVE Temperature Control Strategy

This section defines the Occupancy-Based System for Efficient Reduction of hVac Energy (OBSERVE) predictive control algorithm, which uses a BMC to predictively condition room temperature. The function $BMC(OccState, predLen)$ return a predicted schedule of occupancy $occPred$, where $occPred_t$ is a probability a space being occupied at time $t = 1 \dots predLen$ and $OccState$ is the occupancy state at time $t = 0$. This conditioning strategy is also applicable for binary occupancy data. The BMC can be easily adapted to binary data by representing the MC state at each time as a vector where each component is a binary indication of occupancy (instead of actual occupancy). Algorithm 1 defines the OBSERVE temperature control strategy.

This strategy conditions for two different types of occupancy. It first checks short windows of time for occupancy to ensures that rooms, such as copy rooms, that are not frequented often but have occupied durations of several minutes are conditioned. The second longer window ensures rooms that are frequented constantly but may have short stay durations are still conditioned. Hallways are an example of such an area. Since no standards currently define what constitutes a significant duration of occupancy, we chose values that seem reasonable.

8. EVALUATED STRATEGIES

Four different strategies are considered. The first is coefficient based baseline strategy that employs a typical HVAC control strategy assuming maximum occupancy for ventila-

EnergyPlus Building Parameters

HVAC	Single Duct AHU, VAV with terminal reheat Gas heating and cooling 9 zones
Temperature Setbacks	Heating: $T_{tg} = 75^\circ\text{F}$, $T_{ASH} = 70^\circ\text{F}$ Cooling: $T_{tg} = 78^\circ\text{F}$, $T_{ASH} = 82^\circ\text{F}$
Areas	Total: 30,130 ft ²
Materials	Concrete exterior walls Metal interior walls 30% double glazed windows

Table 1: Main building parameters used.

tion and conditions all rooms from 7:00 - 22:00. The second strategy is a binary based reactive control of temperature and ventilation. Rooms are conditioned to a target temperature when occupied and are not predictively preconditioned. Rooms that are unoccupied are still conditioned to the max/min temperatures allowed by ASHRAE. Since precise room occupancies are unknown, rooms are ventilated according to the estimated maximum occupancy when occupied. The maximum occupancy is determined using ASHRAE Standard 62.1 based on area and room purpose. The third strategy uses the OBSERVE algorithm described in Section 7.2. Ventilation is based on the observed room occupancy using equation 4 during warm months (Apr - Oct). During the colder months ventilation rates are increased. This increased ventilation is an optimization for terminal reheat HVAC system and is discussed in Section 9.2.1. The last strategy uses the OBSERVE algorithm but uses binary data to train the BMC model. This strategy makes binary predictions of occupancy and ventilates with the same maximum occupancy assumption of the reactive control strategy.

9. PERFORMANCE RESULTS

9.1 Building Energy Simulator

EnergyPlus is one of the premiere tools for modeling the energy of buildings. It takes into account factors such as weather, HVAC design, and construction materials. In this section we define the main parameters used for an EnergyPlus model to test our HVAC strategies.

9.1.1 Building Parameters

EnergyPlus simulations are run for three different locations; Fresno CA, Miami FL, and Chicago IL. The EnergyPlus model replicates the geometry shown in Figure 1 and is constructed to ASHRAE standards. Table 1 summarizes the main model parameters. The HVAC is a terminal reheat system that uses a single air handler unit (AHU) with variable air volume vents (VAV). The sizing of the AHU is done according to ASHRAE Standard 62.1 [4]. This type of HVAC system cools air at the AHU level and heats primarily at the VAV level. This is common for many office buildings [9]. This type of system is often used since it is able to heat and cool areas while still sharing the same AHU. We save the evaluation of other types of HVAC systems for future work. The set-points correspond the temperatures that predict $-0.5 \leq \text{PMV} \leq 0.5$ assuming 40% humidity, 1 m/s airflow, and clothing coefficients of 1.0 and 0.5 for winter and summer respectively. Fresno, Miami, and Chicago have 40%, 52%, and 32% average humidities respectively. The HVAC system controls humidity to be between 35% and 45% using a cool-reheat heating coil.

9.1.2 Simulated Occupancy Schedules

EnergyPlus models typically use static occupancy schedules specified in sources such as ASHRAE 90.1 and DOE-2 [1] and are often based on survey data. For our model, however, we will use the BMC to generate occupancy schedules. A BMC trained with 5 days of ground truth data is used to generate 23 days of simulated ‘‘ground truth’’ occupancy data for the building model. These simulations will serve as our occupancy schedules for the weekdays of the month. The building is assumed to be empty on weekends. Static occupancy schedules are used for the restrooms since we have no data for privacy reasons.

Our control strategy assumes a system similar to SCOPES for occupancy monitoring. For 20% of the time, the system inverts the direction or detects a false positive or negative transition. We simulate SCOPES system error by artificially introducing errors into the simulated ground truth data. Because directional errors occur with roughly the same frequency, even with 80% accuracy, the observed system data is close to ground truth. Since errors may produce states that do not exist in the BMC, the closest distance metric defined earlier is used to find the closest state for the OBSERVE algorithm. Figure 10 compares the simulated scopes with the simulated ground truth.

9.2 Energy Savings

We evaluate the energy savings possible using the defined HVAC strategies for each location. These results take into account the fan, pump, heating (gas), and cooling (gas) energy consumption of the building. Figure 11 shows the monthly breakdown of the energy consumption for each location. Significant energy savings are achievable over a standard commonly used baseline; we see up to 112% improvement in some cases. We see that heating and cooling account for most of the energy usage and that heating requires more energy than cooling. OBSERVE Occupancy out-performs binary strategies. The strategies have the most substantial savings during the colder months. This is primarily because heating costs are greater than cooling costs.

During the coldest months in Fresno, the strategies are 45%-47% more efficient than baseline; in particular OBSERVE Occupancy shows 88% to 112% improvement over baseline. For Fresno, OBSERVE Occupancy, OBSERVE Binary, and Reactive Binary show annual savings of 42.3%, 38.3%, and 37.9% respectively. Similar results are found for the Chicago location. The difference among strategies increases during the warmer summer months. For summer months in Fresno, OBSERVE Occupancy shows 9%-11% improvement over Reactive Binary and 7%-10% improvement over OBSERVE binary. For summer months in Chicago, OBSERVE Occupancy shows 10%-12% improvement over Reactive Binary, and 6%-7% improvement over OBSERVE Binary. This suggests OBSERVE Occupancy is more efficient for warm weather areas. When we examine the results from the warmer Miami location, OBSERVE Occupancy shows 11%- 18% improvement over both binary strategies throughout the year. OBSERVE Occupancy again shows significant improvement over baseline (33%-69%). We see that OBSERVE Occupancy is 26%-41% more efficient than baseline whereas Reactive Binary is 17%-30% more efficient. OBSERVE Occupancy, OBSERVE Binary, and Reactive Binary have annual savings of 30.4%, 23.7%, and 21.4% respectively for Miami.

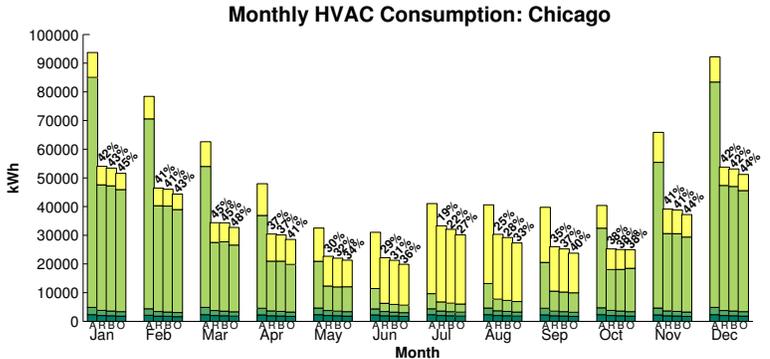
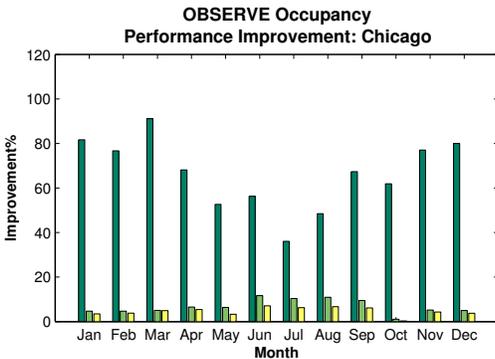
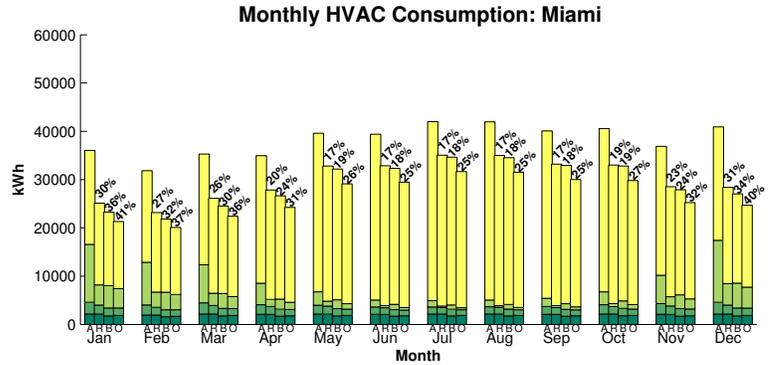
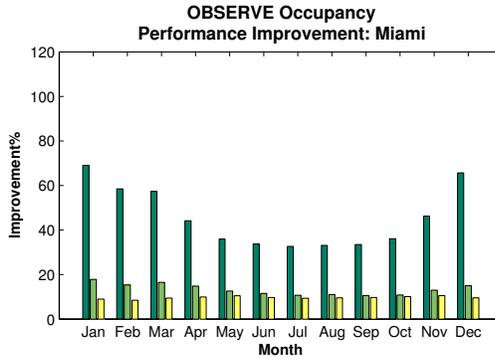
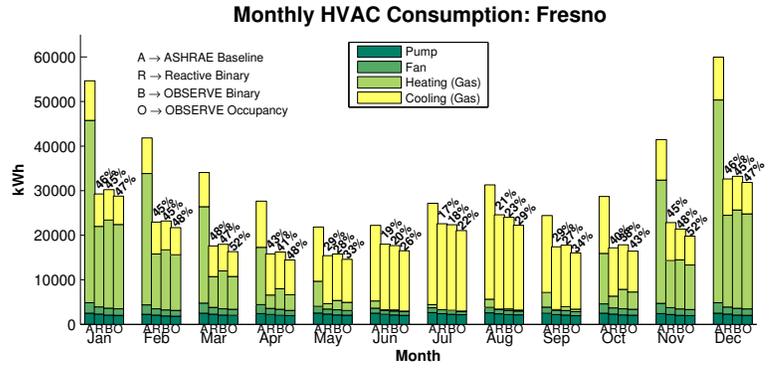
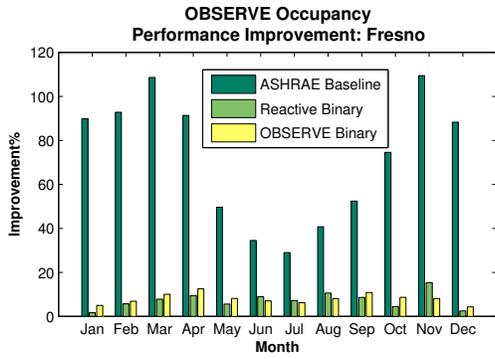


Figure 11: The breakdown of the energy consumption for each month and strategy for three different locations.

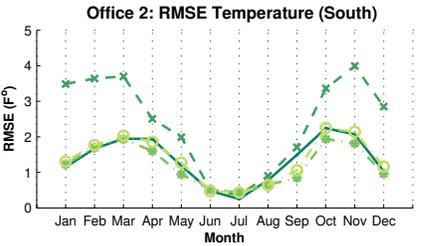
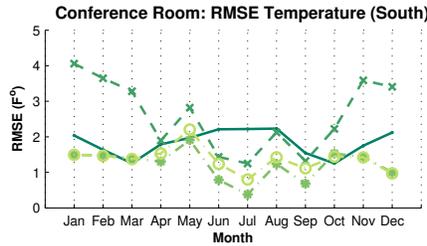
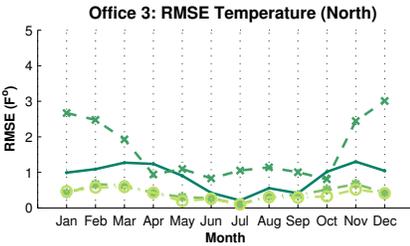
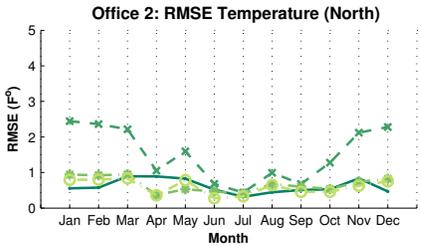
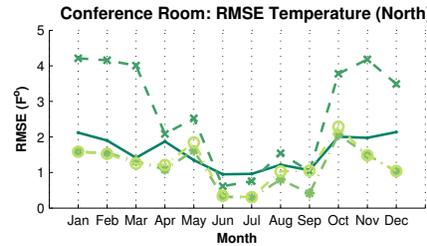
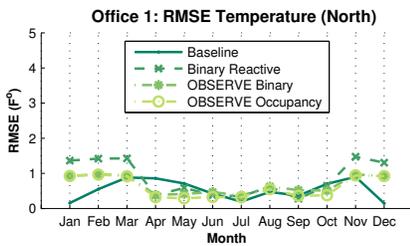


Figure 12: Monthly RMSE temperature for each strategy for Fresno.

9.2.1 Discussion

We see that all three strategies are significantly more efficient than baseline and that there are noticeable differences among the strategies. The main source of these differences is related to ventilation and the terminal reheat system used for the building. OBSERVE Occupancy is able to adjust the ventilation rate according to estimated occupancy whereas OBSERVE Binary and Binary Reactive use the maximum ventilation rate during periods of occupancy. Typically, increasing the ventilation rate introduces additional outside air into the air handler loop and increases the energy consumption since the outside air needs to be conditioned; recirculating air is more efficient since it takes less energy to maintain pre-conditioned air. However, there are other ventilation efficiency factors that need to be considered with a terminal reheat system. A terminal reheat system partially preheats outside air before entering the AHU then reheats air at the room VAV. Under certain conditions, it is more efficient to increase ventilation. Increasing ventilation means losing some energy since more outside air needs to be conditioned. However, increased ventilation distributes the heating load across all the VAV's and increases the amount of VAV pre-heated air into the loop. Based on EnergyPlus simulations, we found increased ventilation during cold months increases efficiency. The same is not true for cooling. Since cooling is done completely at the AHU level, the VAV's can no longer be recruited to help distribute the load and any additional ventilation decreases efficiency. The significant improvement of OBSERVE Occupancy over the binary strategies in Miami confirms this. Thus, an HVAC system that does all the conditioning in the AHU will benefit the most from optimal venting. This could be achieved in many terminal reheat systems by increasing the AHU preheating.

9.3 Conditioning Effectiveness

While substantial energy savings are possible, we must verify the building is ASHRAE compliant. For this analysis we focus on the Fresno EnergyPlus simulations.

9.3.1 Temperature Effectiveness

We examine the temperature of the rooms during all times of occupancy. In particular, we are interested in areas such as the Conference Room, which are not occupied the majority of the day. In order to be ASHRAE [3] compliant, we must maintain the set-point temperatures to ensure $-0.5 \leq PMV \leq 0.5$. As mentioned before, we examine temperature directly rather than PMV; our goal is to meet the temperature set by any metric of thermal comfort. For this analysis, we examine the root mean square error (RMSE) of the room temperatures. We also examine building orientation to observe the influence of solar gain.

All four strategies perform similarly for Office 1. Reactive Binary has the highest RMSE (1.3°) for Nov-Mar. Both OBSERVE strategies have similar results throughout the year. Baseline performed best during the coldest months.

OBSERVE Occupancy performs the best out of the four strategies for Office 3 with a RMSE of 0.1-0.3 F°. OBSERVE Binary has a slightly higher RMSE of 0.1-0.5 F°. The Reactive Binary strategy is highest with a RMSE of 0.9-2.8 F°. For Dec-Jan Reactive Binary has a RMSE of 2.5 F° as compared with the RMSE of 0.1 F° and 1.0 F° for OBSERVE Occupancy and baseline respectively.

Two different building orientations are considered for Con-

ference Room and Office 2 to show the effect of solar gain. North is defined in Figure 1. South refers to the building turned 180°. Reactive Binary has higher RMSE for the south orientation (0.4-3.6 F°) than the north orientation (0.2-2.4 F°). Both OBSERVE strategies have lower RMSE than Reactive Binary for both orientations. Generally, both OBSERVE strategies have slightly lower RMSE than baseline for the north orientation. Both OBSERVE strategies show higher RMSE for the south orientation than the north orientation; this is caused by solar gain.

For the Conference Room, Reactive Binary has higher RMSE during the colder months (4.0-4.2 F°) for both orientations. During the summer, Reactive Binary has higher RMSE for the south orientation. For the north orientation, the baseline does better than OBSERVE strategies for winter and spring. During the summer, however, both OBSERVE strategies have lower RMSE than baseline. Comparing OBSERVE strategies, OBSERVE Binary has lower RMSE than OBSERVE Occupancy for the summer south orientation (0.3-1.1 F° vs 0.8-1.2 F°).

9.3.2 Discussion

Reactive Binary tends to have higher RMSE than the other strategies because of the slow ramp up to target temperature. Once an occupant enters a room, it takes time to reach the target temperature. For areas occupied most of the time such as Office 1, Reactive Binary performance improves but does not match quality of service of predictive strategies since there is still a temperature reaction delay at the beginning of the day when the first occupant enters. This delay becomes more critical for areas sporadically occupied such as Office 2 and the Conference Room. A room occupied once or twice a day, such as the Conference Room has insufficient time to reach the target temperature and is only at the correct temperature if the outside conditions happens to match the target temperature (spring, fall). RMSE increases if the room receives afternoon sun as is shown for the southern orientation of the Conference Room and Office 2. Rooms such as Office 2 that are constantly visited have slightly lower RMSE since the thermal momentum creates an additive effect that helps maintain temperature. These results show that reactive strategies based on a PIR WSN *do not work in practice and cannot reach the target temperature* required by the users for all the different scenarios tested.

In some cases, OBSERVE strategies perform better than the baseline since the baseline uses a static HVAC schedule. This is seen for Office 3, which is occupied by professors and graduate students working at odd hours. The static baseline schedule stops conditioning during normal working hours whereas OBSERVE anticipates after hours usage. Even Reactive Binary out-performs the baseline during mild months (spring and fall) when rooms are occupied off-hours and the outside and target temperatures are close.

Both OBSERVE strategies perform similarly. However, there are instances in warm weather where OBSERVE Binary performs slightly better. This is related to over ventilation. Assuming maximum occupancy forces the VAV vent to open fully when conditioning a room and less time is required to cool the room. The same is not true for heating since air from the loop is only partially preheated.

9.3.3 Ventilation Effectiveness

The minimum ventilation rate is established by Equation 4. Since the occupancy detection system can under-

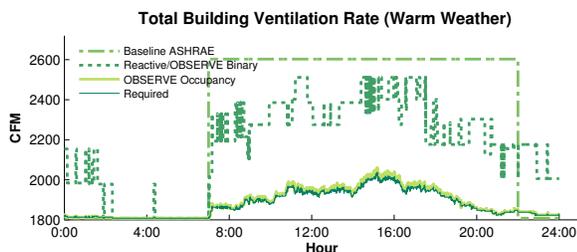


Figure 13: Total building ventilation rates for each strategy for one particular summer day.

count occupants, we add an additional 10% to occupancy estimates. Figure 13 shows the ventilation rate for a summer day. The baseline strategy assumes a maximum ventilation rate. The binary strategies use a maximum ventilation rate only when an area is occupied. OBSERVE Occupancy uses a modified schedule. It uses maximum ventilation during cold months (Oct-Apr for Fresno/Chicago) and optimal ventilation during the warm months (year-round for Miami). From the summer day ventilation, we can see that the baseline greatly over-ventilates the building. While binary based strategies are an improvement, we can see that binary ventilation rate far exceeds the required ventilation rate. It has a RMSE of 335.0 CFM (Normalized RMSE of 146%). OBSERVE however, remains close to the required ventilation rate and has a RMSE of 9.5 CFM (NRMSE of 4.1%). OBSERVE is usually above the required ventilation because of the 10% safety margin for under-counting. OBSERVE fell below the required ventilation rate only 0.0004% of the time. From Oct-Apr, both binary and OBSERVE share the same ventilation rates and have a NRMSE of 146%.

10. CONCLUSIONS AND FUTURE WORK

We propose a statistical model of the temporal occupancy of a building based on an inhomogeneous Markov chain estimated from occupancy data collected from a sensor network. We control the complexity of the state space by using only states observed during training, and prevent discontinuities in the chain by a closest distance Markov chain (CDMC) approach, or by continuously blending the transition matrices over time (BMC). Comparing samples generated from the model with ground-truth data using various metrics shows that the model captures the occupancy dynamics accurately. We have also shown how the model can be integrated with a WSN for demand control based conditioning strategies. We propose the OBSERVE predictive demand control strategy and test the energy savings and conditioning performance. We learned several lessons from our results. First, in order to achieve energy savings, *real time occupancy data is critical*. This can be seen by the average 42% annual energy savings compared to the current state of the art baseline strategy. Second, *predictive* strategies show better energy savings performance and even *significantly* better quality of service conditioning than reactive strategies. Finally, in order to achieve *maximum* energy savings, *actual level of occupancy* is required in order to optimize ventilation levels. For future work, we plan to deploy a new occupancy estimation system on two floors and train the model in real time over longer period of time. Once deployed we can integrate OBSERVE into the HVAC system and refine the OBSERVE algorithm to optimally determine precondition times.

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